



**NAMIBIA UNIVERSITY**  
OF SCIENCE AND TECHNOLOGY

**FACULTY OF MANAGEMENT SCIENCES**

**DEPARTMENT OF MARKETING AND LOGISTICS**

|   |                                    |
|---|------------------------------------|
| <b>QUALIFICATION:</b> BACHELOR OF LOGISTICS AND SUPPLY CHAIN MANAGEMENT HONOURS |                                    |
| <b>QUALIFICATION CODE:</b> 08HLSCH  | <b>LEVEL:</b> 8                    |
| <b>COURSE:</b> FINANCIAL TECHNIQUES FOR LOGISTICS MANAGEMENT OPERATIONS         | <b>COURSE CODE:</b> FTL 821S       |
| <b>SESSION:</b> JANUARY 2020  | <b>PAPER:</b> THEORY AND PRACTICAL |
| <b>DURATION:</b> 3 HOURS  | <b>MARKS:</b> 100                  |

| <b>SECOND OPPORTUNITY EXAMINATION QUESTION PAPER</b> |                              |
|--|------------------------------|
| <b>EXAMINER</b>                                      | Mr. T. Nakweenda (UNAM)      |
| <b>MODERATOR:</b>                                    | Mr. Johannes Ndjuluwa (UNAM) |

| <b>INSTRUCTIONS</b>   |
|---|
| 1. Answer all questions.<br>2. Number your answers accordingly.<br>3. The use of PV and FV tables attached as appendix is permissible.<br>4. Round your answers to four decimal places wherever applicable. |

**THIS QUESTION PAPER CONSISTS OF 6 PAGES** (Including this front page)

**Question 1 (10 Marks, 18 Minutes)**

| <b>REQUIRED:</b>  | <b>MARKS</b> |
|---|--------------|
| 1.1. What is the primary role of a financial manager?   | 4            |
| 1.2. Briefly describe the nature of principal-agent relationship between the owners and managers of a corporation. Clearly explain how various corporate governance mechanisms attempt to manage agency problems. | 6            |
| <b>TOTAL MARKS FOR QUESTION 1</b>   | <b>10</b>    |

**Question 2 (30 Marks, 54 Minutes)**

This question is divided into two parts, namely: 2.1 and 2.2, which are independent of each other. Under each part, try to answer the questions in the context in which they have been asked. Be concise as much as possible.

**2.1.**

Suppose you have been provided with the following information which was extracted from records of ABC Ltd.

| <b>Statement of Financial Statement</b> | <b>2018</b>      | <b>2017</b>      |
|---|------------------|------------------|
| Share capital (par value N\$ 2)         | 200 000          | 200 000          |
| Retained earnings                       | 510 000          | 490 000          |
| Long term liabilities                   | 424 000          | 250 000          |
| Trade and other payables                | 66 000           | 60 000           |
| <b>Total equity and liabilities</b>     | <b>1 200 000</b> | <b>1 000 000</b> |
|   |                  |                  |
| <b>Non-current assets</b>               |                  |                  |
| Plant and equipment at cost             | 1 480 000        | 1 200 000        |
| Accumulated depreciation                | (560 000)        | (500 000)        |
| Net non-current assets                  | 920 000          | 700 000          |
|   |                  |                  |
| <b>Current assets</b>                   |                  |                  |

|                             |                  |                  |
|-----------------------------|------------------|------------------|
| Inventory                   | 150 000          | 150 000          |
| Trade and other receivables | 120 000          | 100 000          |
| Cash                        | 10 000           | 50 000           |
| <b>Total current assets</b> | <b>280 000</b>   | <b>300 000</b>   |
|                             |                  |                  |
| <b>Total Assets</b>         | <b>1 200 000</b> | <b>1 000 000</b> |

| <b>Statement of Comprehensive Income</b>    |                |                |
|---|----------------|----------------|
|   | <b>2018</b>    | <b>2017</b>    |
| Sales (40% cash sales)                      | 1 200 000      | 1 080 000      |
| Cost of sales                               | 900 000        | 842 000        |
| <b>Gross profit</b>                         | <b>300 000</b> | <b>238 000</b> |
| Operating expenses                          | 114 000        | 104 000        |
| Depreciation                                | 60 000         | 32 000         |
| <b>Net profit before interest and taxes</b> | <b>126 000</b> | <b>102 000</b> |
| Interest                                    | 39 600         | 23 000         |
| <b>Net profit before taxes</b>              | <b>86 400</b>  | <b>79 000</b>  |
| Taxes @ 30%                                 | 25 920         | 23 700         |
| <b>Net profit after tax</b>                 | <b>60 480</b>  | <b>55 300</b>  |

| <b>REQUIRED: Compute and comment on the following ratios for both years.</b> |                          | <b>MARKS</b> |
|--|--------------------------|--------------|
| 2.1.1.   | Total debt ratio         | 2            |
| 2.1.2.   | Inventory turnover ratio | 4            |
| 2.1.3.   | Days sales in inventory  | 4            |
| 2.1.4.   | Days sales in payables   | 4            |
| 2.1.5.   | Net profit on sales      | 2            |
| <b>TOTAL MARKS FOR 2.1.</b>  |                          | <b>16</b>    |

2.2.

Your uncle wants to start investing N\$ 5 000 every year for the next five years of which he could earn 10% interest per annum. He is currently not sure whether to invest at the end or beginning of each year.

| <b>REQUIRED:</b>   | <b>MARKS</b> |
|--|--------------|
| <b>2.2.1.</b> Differentiate between an annuity due and ordinary annuity. Use the given scenario to substantiate your answer. | 2            |
| <b>2.2.2.</b> Which of the two options would you recommend to your uncle? Clearly show the difference in benefits.           | 12           |
| <b>TOTAL MARKS FOR 2.2</b>   | <b>14</b>    |
| <b>TOTAL MARKS FOR QUESTION 2</b>  | <b>30</b>    |

### **Question 3 (25 Marks, 45 Minutes)**

This question is divided into two parts, namely: 3.1 and 3.2, which are independent of each other. Under each part, try to answer the questions in the context in which they have been asked. Be concise as much as possible.

#### **3.1. (10 Marks, 18 Minutes)**

Ms. Pretty is contemplating to buy a share in one of the local equity brokers which has the following features:

- Free risk rate 5%
- Market expected rate of return 16%
- Beta factor 1.1

| <b>REQUIRED:</b>  | <b>MARKS</b> |
|---|--------------|
| <b>3.1.1.</b> Using the Capital Asset Pricing Model (CAPM), what would be your recommendation to Ms. Pretty?  | 5            |
| <b>3.1.2.</b> Ms. Elna, a close ally of Ms. Pretty has this to say: My friend, if I were you, I would only invest in that share if its market expected rate of return falls to 12% with a beta factor of 0.8. I expect the risk free rate to remain the same – <i>Ms. Elna narrates to her friend</i> . What is your take on Ms. Elna's sentiments? Clearly show all your workings. | 5            |
| <b>TOTAL MARKS FOR 3.1.</b>   | <b>10</b>    |

#### **3.2. (15 Marks, 27 Minutes)**

Company XYZ Ltd just paid a dividend of 60c per share. Shareholders demands a return of 12% p.a. Growth for the next 3 years are expected to be 30% and after that growth will stabilize at 6% p.a.

|  |  |              |
|--|--|--------------|
|  | <b>REQUIRED: Clearly show all your workings.</b> | <b>MARKS</b> |
|--|--|--------------|

|                                   |  |           |
|-----------------------------------|--|-----------|
| <b>3.2.1.</b>                     | Using the information above, determine the value of company XYZ Ltd share today. | 10        |
| <b>3.2.2.</b>                     | Why do you think companies pay out dividends?                                    | 5         |
| <b>TOTAL MARKS FOR 3.2.</b>       |  | <b>15</b> |
| <b>TOTAL MARKS FOR QUESTION 3</b> |  | <b>25</b> |

#### **Question 4 (15 Marks, 27 Minutes)**

Mr Oloman is the financial manager of Pick 'n Pay Ltd (Pick 'n Click), a subsidiary company of a large food chain in Namibia. He is responsible for the acquisition of new companies for the group and identified Food Lovers (Pty) Ltd (Food Lovers) as a potential acquisition.

Mr Oloman calculated the weighted average cost of capital to assist him in making his acquisition decision of Food Lovers. Pick 'n Pay has a target capital structure of 50% equity, 20% preference shares and 30% debentures.

The current market values of all sources of financing of Pick 'n Pay are as follows:

| Source of finance                    | Notes | Market value (N\$) |
|--------------------------------------|-------|--------------------|
| Equity                               | 1     | 12 321 000         |
| 12% non-redeemable preference shares | 2     | 1 596 000          |
| 8% redeemable debentures             | 3     | 5 897 000          |
| Long-term loan                       | 4     | 1 650 000          |
| Bank overdraft                       | 5     | 520 000            |

#### **Notes:**

1. The company has authorised share capital of 500 000 ordinary shares of which 320 000 have been issued. A dividend of N\$ 5.40 per ordinary share has just been paid and it is expected that dividends will grow at 3% per year and that the growth will remain constant in the future.
2. 100 000 Preference shares are in issue. The current market related return on similar preference shares is 10% before tax.
3. The company has 65 000 debentures in issue that are redeemable in 9 years at a premium of 5%. Interest is payable annually. The interest rate of similar debentures is currently 9.5% before tax.
4. The long-term loan is payable over 2 years in two equal instalments. The loan bears interest at 14% per year and will not be renewed once it has been paid off.

5. The company has a bank overdraft that bears interest at prime + 4%. The bank overdraft is only used if the company experiences cash flow problems.
6. The current tax rate applicable to Pick 'n Pay is 28%. All other taxes can be ignored.

Mr Oloman made the following weighted average cost of capital calculation:

|                   | N\$               | Weight | Cost   | Weighted cost |
|-------------------|-------------------|--------|--------|---------------|
| Equity*           | 12 321 000        | 56.05% | 17.03% | 9.54%         |
| Preference shares | 1 596 000         | 7.26%  | 10%    | 0.73%         |
| Debentures        | 5 897 000         | 26.82% | 9.5%   | 2.55%         |
| Long-term loan*   | 1 650 000         | 7.51%  | 10.08% | 0.76%         |
| Bank overdraft    | 520 000           | 2.37%  | 13.25% | 0.31%         |
|                   | <b>21 984 000</b> |        |        | <b>13.89%</b> |

**\*Calculations:**

**Cost of equity**

$$Ke = (R5.40/R38.50) + 0.03 \\ = 17.03\%$$

**Cost of long-term loan**

$$Kd = 14\% \times 72\% \\ = 10.08\%$$

| <b>REQUIRED: Clearly show all your workings:</b> |  | <b>MARKS</b> |
|--|--|--------------|
| 4.1.   | Advise Mr. Oloman on whether his calculation relating to the weighted average cost of capital is correct. If not, provide reasons for your answer as well as the correct calculations. | 10           |
| 4.2.   | Why do you think WACC is considered one of the useful indicators for investment decisions?   | 5            |
| <b>TOTAL MARKS FOR QUESTION 4</b>                |  | <b>15</b>    |

**Question 5 (20 Marks, 36 Minutes)**

Selma has just successfully completed her course in Logistics and Supply Chain Management from NUST. As a way of putting her theory into practice, she is contemplating to come up with a recreational centre in her area where residents could go to for recreational purposes. The project would cost N\$ 150 000 to implement, and it would have a useful life of five years with a zero residual value. She would expect the project to generate after tax cash inflows of N\$ 35

500 per annum for the first three years and N\$ 32 000 per annum for the reminder years of its useful life. Similar investments require an expected rate of return of 12% per annum.

| <b>REQUIRED:</b>  | <b>MARKS</b> |
|---|--------------|
| 5.1. On the basis of Net Present Value (NPV), would it be sensible for Selma to go ahead with her idea?   |              |
| 5.2. Suppose you have further been provided with the following information: applicable corporate tax rate is 30% and a residual value of N\$ 20 000. Determine Selma's Accounting Rate of Return (ARR). Clearly show all your workings. It is Selma's prerogative decision to only accept projects with a minimum ARR of 65%. On the basis of ARR, should Selma go ahead with her decision? |              |
| 5.3. With the help of your answers in 5.1 and 5.2, are there any conflicting answers? If so, on the basis of the two techniques, which one would you recommend to Selma and why?  |              |
| <b>TOTAL MARKS FOR QUESTION 5</b>   | <b>20</b>    |

Future value interest factor of \$1 at i% for n periods,  $FVIF(i,n) = \$1 * (1+i)^n$

| Period | 1%    | 2%    | 3%    | 4%    | 5%     | 6%     | 7%     | 8%     | 9%     | 10%     | 11%     | 12%     | 13%     | 14%     | 15%       | 16%       | 17%       | 18%       | 19%       | 20%       |
|--------|-------|-------|-------|-------|--------|--------|--------|--------|--------|---------|---------|---------|---------|---------|-----------|-----------|-----------|-----------|-----------|-----------|
| 1      | 1.010 | 1.020 | 1.030 | 1.040 | 1.050  | 1.060  | 1.070  | 1.080  | 1.090  | 1.100   | 1.110   | 1.120   | 1.130   | 1.140   | 1.150     | 1.160     | 1.170     | 1.180     | 1.190     | 1.200     |
| 2      | 1.020 | 1.040 | 1.061 | 1.082 | 1.103  | 1.124  | 1.145  | 1.166  | 1.188  | 1.210   | 1.232   | 1.254   | 1.277   | 1.300   | 1.323     | 1.346     | 1.369     | 1.392     | 1.416     | 1.440     |
| 3      | 1.030 | 1.061 | 1.093 | 1.125 | 1.158  | 1.191  | 1.225  | 1.260  | 1.295  | 1.331   | 1.368   | 1.405   | 1.443   | 1.482   | 1.521     | 1.561     | 1.602     | 1.643     | 1.685     | 1.728     |
| 4      | 1.041 | 1.082 | 1.126 | 1.170 | 1.216  | 1.262  | 1.311  | 1.360  | 1.412  | 1.464   | 1.518   | 1.574   | 1.630   | 1.689   | 1.749     | 1.811     | 1.874     | 1.939     | 2.005     | 2.074     |
| 5      | 1.051 | 1.104 | 1.159 | 1.217 | 1.276  | 1.338  | 1.403  | 1.469  | 1.539  | 1.611   | 1.685   | 1.762   | 1.842   | 1.925   | 2.011     | 2.100     | 2.192     | 2.288     | 2.386     | 2.488     |
| 6      | 1.062 | 1.126 | 1.194 | 1.265 | 1.340  | 1.419  | 1.501  | 1.587  | 1.677  | 1.772   | 1.870   | 1.974   | 2.082   | 2.195   | 2.313     | 2.436     | 2.565     | 2.700     | 2.840     | 2.986     |
| 7      | 1.072 | 1.149 | 1.230 | 1.316 | 1.407  | 1.504  | 1.606  | 1.714  | 1.828  | 1.949   | 2.076   | 2.211   | 2.353   | 2.502   | 2.660     | 2.826     | 3.001     | 3.185     | 3.379     | 3.583     |
| 8      | 1.083 | 1.172 | 1.267 | 1.369 | 1.477  | 1.594  | 1.718  | 1.851  | 1.993  | 2.144   | 2.305   | 2.476   | 2.658   | 2.853   | 3.059     | 3.278     | 3.511     | 3.759     | 4.021     | 4.300     |
| 9      | 1.094 | 1.195 | 1.305 | 1.423 | 1.551  | 1.688  | 1.838  | 1.999  | 2.172  | 2.358   | 2.558   | 2.773   | 3.004   | 3.252   | 3.518     | 3.803     | 4.108     | 4.435     | 4.785     | 5.160     |
| 10     | 1.105 | 1.219 | 1.344 | 1.480 | 1.629  | 1.791  | 1.967  | 2.159  | 2.367  | 2.594   | 2.839   | 3.106   | 3.395   | 3.707   | 4.046     | 4.411     | 4.807     | 5.234     | 5.695     | 6.192     |
| 11     | 1.116 | 1.243 | 1.384 | 1.539 | 1.710  | 1.898  | 2.105  | 2.332  | 2.580  | 2.853   | 3.152   | 3.479   | 3.836   | 4.226   | 4.652     | 5.117     | 5.624     | 6.176     | 6.777     | 7.430     |
| 12     | 1.127 | 1.268 | 1.426 | 1.601 | 1.796  | 2.012  | 2.252  | 2.518  | 2.813  | 3.138   | 3.498   | 3.896   | 4.335   | 4.818   | 5.350     | 5.936     | 6.580     | 7.288     | 8.064     | 8.916     |
| 13     | 1.138 | 1.294 | 1.469 | 1.665 | 1.886  | 2.133  | 2.410  | 2.720  | 3.066  | 3.452   | 3.883   | 4.363   | 4.898   | 5.492   | 6.153     | 6.886     | 7.699     | 8.599     | 9.596     | 10.699    |
| 14     | 1.149 | 1.319 | 1.513 | 1.732 | 1.980  | 2.261  | 2.579  | 2.937  | 3.342  | 3.797   | 4.310   | 4.887   | 5.535   | 6.261   | 7.076     | 7.988     | 9.007     | 10.147    | 11.420    | 12.839    |
| 15     | 1.161 | 1.346 | 1.558 | 1.801 | 2.079  | 2.397  | 2.759  | 3.172  | 3.642  | 4.177   | 4.785   | 5.474   | 6.254   | 7.138   | 8.137     | 9.266     | 10.539    | 11.974    | 13.590    | 15.407    |
| 16     | 1.173 | 1.373 | 1.605 | 1.873 | 2.183  | 2.540  | 2.952  | 3.426  | 3.970  | 4.595   | 5.311   | 6.130   | 7.067   | 8.137   | 9.358     | 10.748    | 12.330    | 14.129    | 16.172    | 18.488    |
| 17     | 1.184 | 1.400 | 1.653 | 1.948 | 2.292  | 2.693  | 3.159  | 3.700  | 4.328  | 5.054   | 5.895   | 6.866   | 7.986   | 9.276   | 10.761    | 12.468    | 14.426    | 16.672    | 19.244    | 22.186    |
| 18     | 1.196 | 1.428 | 1.702 | 2.026 | 2.407  | 2.854  | 3.380  | 3.996  | 4.717  | 5.560   | 6.544   | 7.690   | 9.024   | 10.575  | 12.375    | 14.463    | 16.879    | 19.673    | 22.901    | 26.623    |
| 19     | 1.208 | 1.457 | 1.754 | 2.107 | 2.527  | 3.026  | 3.617  | 4.316  | 5.142  | 6.116   | 7.263   | 8.613   | 10.197  | 12.056  | 14.232    | 16.777    | 19.748    | 23.214    | 27.252    | 31.948    |
| 20     | 1.220 | 1.486 | 1.806 | 2.191 | 2.653  | 3.207  | 3.870  | 4.661  | 5.604  | 6.727   | 8.062   | 9.646   | 11.523  | 13.743  | 16.367    | 19.461    | 23.106    | 27.393    | 32.429    | 38.338    |
| 25     | 1.282 | 1.641 | 2.094 | 2.666 | 3.386  | 4.292  | 5.427  | 6.848  | 8.623  | 10.835  | 13.585  | 17.000  | 21.231  | 26.462  | 32.919    | 40.874    | 50.658    | 62.669    | 77.388    | 95.396    |
| 30     | 1.348 | 1.811 | 2.427 | 3.243 | 4.322  | 5.743  | 7.612  | 10.063 | 13.268 | 17.449  | 22.892  | 29.960  | 39.116  | 50.950  | 66.212    | 85.850    | 111.065   | 143.371   | 184.675   | 237.376   |
| 35     | 1.417 | 2.000 | 2.814 | 3.946 | 5.516  | 7.686  | 10.677 | 14.785 | 20.414 | 28.102  | 38.575  | 52.890  | 72.069  | 98.100  | 133.176   | 180.314   | 243.503   | 327.997   | 440.701   | 590.668   |
| 40     | 1.489 | 2.208 | 3.262 | 4.801 | 7.040  | 10.286 | 14.974 | 21.725 | 31.409 | 45.259  | 65.001  | 93.051  | 132.782 | 188.884 | 267.864   | 378.721   | 533.899   | 750.378   | 1.051.668 | 1.469.772 |
| 50     | 1.645 | 2.692 | 4.384 | 7.107 | 11.467 | 18.420 | 29.457 | 46.902 | 74.358 | 117.391 | 184.565 | 289.002 | 450.736 | 700.233 | 1.083.657 | 1.670.704 | 2.566.215 | 3.927.357 | 5.988.914 | 9.100.438 |

Present value interest factor of \$1 at i% for n periods, PVIF(i,n) =  $(1/(1+i))^n$ .

| Period | 1%    | 2%    | 3%    | 4%    | 5%    | 6%    | 7%    | 8%    | 9%    | 10%   | 11%   | 12%   | 13%   | 14%   | 15%   | 16%   | 17%   | 18%   | 19%   | 20%   |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1      | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |
| 2      | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 |
| 3      | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 |
| 4      | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 |
| 5      | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 |
| 6      | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 |
| 7      | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 |
| 8      | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 |
| 9      | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 |
| 10     | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 |
| 11     | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 |
| 12     | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 |
| 13     | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 |
| 14     | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 |
| 15     | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 |
| 16     | 0.853 | 0.728 | 0.623 | 0.534 | 0.458 | 0.394 | 0.339 | 0.292 | 0.252 | 0.218 | 0.188 | 0.163 | 0.141 | 0.123 | 0.107 | 0.093 | 0.081 | 0.071 | 0.062 | 0.054 |
| 17     | 0.844 | 0.714 | 0.605 | 0.513 | 0.436 | 0.371 | 0.317 | 0.270 | 0.231 | 0.198 | 0.170 | 0.146 | 0.125 | 0.108 | 0.093 | 0.080 | 0.069 | 0.060 | 0.052 | 0.045 |
| 18     | 0.836 | 0.700 | 0.587 | 0.494 | 0.416 | 0.350 | 0.296 | 0.250 | 0.212 | 0.180 | 0.153 | 0.130 | 0.111 | 0.095 | 0.081 | 0.069 | 0.059 | 0.051 | 0.044 | 0.038 |
| 19     | 0.828 | 0.686 | 0.570 | 0.475 | 0.396 | 0.331 | 0.277 | 0.232 | 0.194 | 0.164 | 0.138 | 0.116 | 0.098 | 0.083 | 0.070 | 0.060 | 0.051 | 0.043 | 0.037 | 0.031 |
| 20     | 0.820 | 0.673 | 0.554 | 0.456 | 0.377 | 0.312 | 0.258 | 0.215 | 0.178 | 0.149 | 0.124 | 0.104 | 0.087 | 0.073 | 0.061 | 0.051 | 0.043 | 0.037 | 0.031 | 0.026 |
| 25     | 0.780 | 0.610 | 0.478 | 0.375 | 0.295 | 0.233 | 0.184 | 0.146 | 0.116 | 0.092 | 0.074 | 0.059 | 0.047 | 0.038 | 0.030 | 0.024 | 0.020 | 0.016 | 0.013 | 0.010 |
| 30     | 0.742 | 0.552 | 0.412 | 0.308 | 0.231 | 0.174 | 0.131 | 0.099 | 0.075 | 0.057 | 0.044 | 0.033 | 0.026 | 0.020 | 0.015 | 0.012 | 0.009 | 0.007 | 0.005 | 0.004 |
| 35     | 0.706 | 0.500 | 0.355 | 0.253 | 0.181 | 0.130 | 0.094 | 0.068 | 0.049 | 0.036 | 0.026 | 0.019 | 0.014 | 0.010 | 0.008 | 0.006 | 0.004 | 0.003 | 0.002 | 0.002 |
| 40     | 0.672 | 0.453 | 0.307 | 0.208 | 0.142 | 0.097 | 0.067 | 0.046 | 0.032 | 0.022 | 0.015 | 0.011 | 0.008 | 0.005 | 0.004 | 0.003 | 0.002 | 0.001 | 0.001 | 0.000 |
| 50     | 0.608 | 0.372 | 0.228 | 0.141 | 0.087 | 0.054 | 0.034 | 0.021 | 0.013 | 0.009 | 0.005 | 0.003 | 0.002 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |

|        |        | Future value interest factor of an ordinary annuity of \$1 per period at i% for n periods, $FVIFA(i,n) = \$1 * (1 + (1 + i)^1 + (1 + i)^2 + \dots + (1 + i)^{(n-1)})$ . |        |        |        |        |        |        |        |         |         |         |         |         |         |         |         |         |         |         |     |
|--------|--------|---|--------|--------|--------|--------|--------|--------|--------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|-----|
| Period |        | 1%  | 2%     | 3%     | 4%     | 5%     | 6%     | 7%     | 8%     | 9%      | 10%     | 11%     | 12%     | 13%     | 14%     | 15%     | 16%     | 17%     | 18%     | 19%     | 20% |
| 1      | 1.000  | 1.000   | 1.000  | 1.000  | 1.000  | 1.000  | 1.000  | 1.000  | 1.000  | 1.000   | 1.000   | 1.000   | 1.000   | 1.000   | 1.000   | 1.000   | 1.000   | 1.000   | 1.000   | 1.000   |     |
| 2      | 2.010  | 2.020   | 2.030  | 2.040  | 2.050  | 2.060  | 2.070  | 2.080  | 2.090  | 2.100   | 2.110   | 2.120   | 2.130   | 2.140   | 2.150   | 2.160   | 2.170   | 2.180   | 2.190   | 2.200   |     |
| 3      | 3.030  | 3.050   | 3.091  | 3.122  | 3.153  | 3.184  | 3.215  | 3.246  | 3.278  | 3.310   | 3.342   | 3.374   | 3.407   | 3.440   | 3.473   | 3.506   | 3.539   | 3.572   | 3.606   | 3.640   |     |
| 4      | 4.060  | 4.122   | 4.184  | 4.246  | 4.310  | 4.375  | 4.440  | 4.506  | 4.573  | 4.641   | 4.710   | 4.779   | 4.850   | 4.921   | 4.993   | 5.066   | 5.141   | 5.215   | 5.291   | 5.368   |     |
| 5      | 5.101  | 5.204   | 5.309  | 5.416  | 5.526  | 5.637  | 5.751  | 5.867  | 5.985  | 6.105   | 6.228   | 6.353   | 6.480   | 6.610   | 6.742   | 6.877   | 7.014   | 7.154   | 7.297   | 7.442   |     |
| 6      | 6.152  | 6.308   | 6.468  | 6.633  | 6.802  | 6.975  | 7.153  | 7.336  | 7.523  | 7.716   | 7.913   | 8.115   | 8.323   | 8.536   | 8.754   | 8.977   | 9.207   | 9.442   | 9.683   | 9.930   |     |
| 7      | 7.214  | 7.434   | 7.662  | 7.898  | 8.142  | 8.394  | 8.654  | 8.923  | 9.200  | 9.487   | 9.783   | 10.089  | 10.405  | 10.730  | 11.067  | 11.414  | 11.772  | 12.142  | 12.523  | 12.916  |     |
| 8      | 8.286  | 8.583   | 8.892  | 9.214  | 9.549  | 9.897  | 10.260 | 10.637 | 11.028 | 11.436  | 11.859  | 12.300  | 12.757  | 13.233  | 13.727  | 14.240  | 14.773  | 15.327  | 15.902  | 16.499  |     |
| 9      | 9.369  | 9.755   | 10.159 | 10.583 | 11.027 | 11.491 | 11.978 | 12.488 | 13.021 | 13.579  | 14.164  | 14.776  | 15.416  | 16.085  | 16.786  | 17.519  | 18.285  | 19.086  | 19.923  | 20.799  |     |
| 10     | 10.462 | 10.950  | 11.464 | 12.006 | 12.578 | 13.181 | 13.816 | 14.487 | 15.193 | 15.937  | 16.722  | 17.549  | 18.420  | 19.337  | 20.304  | 21.321  | 22.393  | 23.521  | 24.709  | 25.959  |     |
| 11     | 11.567 | 12.169  | 12.808 | 13.486 | 14.207 | 14.972 | 15.784 | 16.645 | 17.560 | 18.531  | 19.561  | 20.655  | 21.814  | 23.045  | 24.349  | 25.733  | 27.200  | 28.755  | 30.404  | 32.150  |     |
| 12     | 12.683 | 13.412  | 14.192 | 15.026 | 15.917 | 16.870 | 17.888 | 18.977 | 20.147 | 21.384  | 22.713  | 24.133  | 25.650  | 27.271  | 29.002  | 30.850  | 32.824  | 34.931  | 37.180  | 39.581  |     |
| 13     | 13.809 | 14.680  | 15.618 | 16.627 | 17.713 | 18.882 | 20.141 | 21.495 | 22.953 | 24.523  | 26.212  | 28.029  | 29.859  | 32.089  | 34.352  | 36.766  | 39.404  | 42.424  | 45.244  | 48.497  |     |
| 14     | 14.947 | 15.974  | 17.086 | 18.292 | 19.599 | 21.015 | 22.550 | 24.215 | 26.019 | 27.975  | 30.095  | 32.393  | 34.883  | 37.581  | 40.505  | 43.672  | 47.103  | 50.818  | 54.841  | 59.196  |     |
| 15     | 16.097 | 17.293  | 18.599 | 20.024 | 21.579 | 23.276 | 25.129 | 27.152 | 29.361 | 31.772  | 34.405  | 37.280  | 40.417  | 43.842  | 47.580  | 51.660  | 56.110  | 60.985  | 66.261  | 72.035  |     |
| 16     | 17.258 | 18.639  | 20.157 | 21.825 | 23.657 | 25.673 | 27.888 | 30.324 | 33.003 | 35.950  | 39.190  | 42.753  | 46.672  | 50.980  | 55.717  | 60.925  | 66.649  | 72.939  | 79.850  | 87.442  |     |
| 17     | 18.430 | 20.012  | 21.762 | 23.698 | 25.840 | 28.213 | 30.840 | 33.750 | 36.974 | 40.545  | 44.501  | 48.884  | 53.739  | 59.118  | 65.075  | 71.673  | 78.979  | 87.068  | 96.022  | 105.93  |     |
| 18     | 19.615 | 21.412  | 23.414 | 25.645 | 28.132 | 30.906 | 33.999 | 37.450 | 41.301 | 45.599  | 50.396  | 55.750  | 61.725  | 68.394  | 75.836  | 84.141  | 93.406  | 103.74  | 115.27  | 128.12  |     |
| 19     | 20.811 | 22.841  | 25.117 | 27.671 | 30.539 | 33.760 | 37.379 | 41.446 | 46.018 | 51.159  | 56.939  | 63.440  | 70.749  | 78.969  | 88.212  | 98.603  | 110.28  | 123.41  | 138.17  | 154.74  |     |
| 20     | 22.019 | 24.297  | 26.870 | 29.778 | 33.066 | 36.786 | 40.995 | 45.762 | 51.160 | 57.275  | 64.203  | 72.052  | 80.947  | 91.025  | 102.44  | 115.38  | 130.03  | 146.63  | 165.42  | 186.69  |     |
| 25     | 28.243 | 32.030  | 36.459 | 41.646 | 47.727 | 54.865 | 63.249 | 73.106 | 84.701 | 98.347  | 114.41  | 133.33  | 155.62  | 181.87  | 212.79  | 249.21  | 292.10  | 342.60  | 402.04  | 471.98  |     |
| 30     | 34.785 | 40.568  | 47.575 | 56.085 | 66.439 | 79.058 | 94.461 | 113.28 | 136.31 | 164.49  | 199.02  | 241.33  | 293.20  | 356.79  | 434.75  | 530.31  | 647.44  | 790.95  | 966.71  | 1,181.9 |     |
| 35     | 41.660 | 49.994  | 60.462 | 73.652 | 90.320 | 111.43 | 138.24 | 172.32 | 215.71 | 271.02  | 341.59  | 431.66  | 546.68  | 693.57  | 881.17  | 1,120.7 | 1,426.5 | 1,816.7 | 2,314.2 | 2,948.3 |     |
| 40     | 48.886 | 60.402  | 75.401 | 95.026 | 120.80 | 154.76 | 199.64 | 259.06 | 337.88 | 442.59  | 581.83  | 767.09  | 1,013.7 | 1,342.0 | 1,779.1 | 2,360.8 | 3,134.5 | 4,163.2 | 5,529.8 | 7,343.9 |     |
| 50     | 64.463 | 84.579  | 112.80 | 152.67 | 209.35 | 290.34 | 406.53 | 573.77 | 815.08 | 1,163.9 | 1,668.8 | 2,400.0 | 3,459.5 | 4,994.5 | 7,217.7 | 10,436  | 15,090  | 21,813  | 31,515  | 45,497  |     |

Present value interest factor of an (ordinary) annuity of \$1 per period at i% for n periods, PVIFA(i,n) =  $\$1 * (1/(1+i) + 1/(1+i)^2 + 1/(1+i)^3 + \dots + 1/(1+i)^n)$ .

| Period | 1%     | 2%     | 3%     | 4%     | 5%     | 6%     | 7%     | 8%     | 9%     | 10%   | 11%   | 12%   | 13%   | 14%   | 15%   | 16%   | 17%   | 18%   | 19%   | 20%   |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1      | 0.990  | 0.980  | 0.971  | 0.962  | 0.952  | 0.943  | 0.935  | 0.926  | 0.917  | 0.909 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |
| 2      | 1.970  | 1.942  | 1.913  | 1.886  | 1.859  | 1.833  | 1.808  | 1.783  | 1.759  | 1.736 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 |
| 3      | 2.941  | 2.884  | 2.829  | 2.775  | 2.723  | 2.673  | 2.624  | 2.577  | 2.531  | 2.487 | 2.444 | 2.402 | 2.361 | 2.322 | 2.283 | 2.246 | 2.210 | 2.174 | 2.140 | 2.106 |
| 4      | 3.902  | 3.808  | 3.717  | 3.630  | 3.546  | 3.465  | 3.387  | 3.312  | 3.240  | 3.170 | 3.102 | 3.037 | 2.974 | 2.914 | 2.855 | 2.798 | 2.743 | 2.690 | 2.639 | 2.589 |
| 5      | 4.853  | 4.713  | 4.580  | 4.452  | 4.329  | 4.212  | 4.100  | 3.993  | 3.791  | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | 3.274 | 3.199 | 3.127 | 3.058 | 2.991 |       |
| 6      | 5.795  | 5.601  | 5.417  | 5.242  | 5.076  | 4.917  | 4.767  | 4.623  | 4.486  | 4.355 | 4.231 | 4.111 | 3.998 | 3.889 | 3.784 | 3.685 | 3.589 | 3.498 | 3.410 | 3.326 |
| 7      | 6.728  | 6.472  | 6.230  | 6.002  | 5.786  | 5.582  | 5.389  | 5.206  | 5.033  | 4.868 | 4.712 | 4.564 | 4.423 | 4.288 | 4.160 | 4.039 | 3.922 | 3.812 | 3.706 | 3.605 |
| 8      | 7.652  | 7.325  | 7.020  | 6.733  | 6.463  | 6.210  | 5.971  | 5.747  | 5.535  | 5.335 | 5.146 | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | 4.207 | 4.078 | 3.954 | 3.837 |
| 9      | 8.566  | 8.162  | 7.786  | 7.435  | 7.108  | 6.802  | 6.515  | 6.247  | 5.995  | 5.759 | 5.537 | 5.328 | 5.132 | 4.946 | 4.772 | 4.607 | 4.451 | 4.303 | 4.163 | 4.031 |
| 10     | 9.471  | 8.983  | 8.530  | 8.111  | 7.722  | 7.360  | 7.024  | 6.710  | 6.418  | 6.145 | 5.889 | 5.650 | 5.426 | 5.216 | 5.019 | 4.833 | 4.659 | 4.494 | 4.339 | 4.192 |
| 11     | 10.368 | 9.787  | 9.253  | 8.760  | 8.306  | 7.887  | 7.499  | 7.139  | 6.805  | 6.495 | 6.207 | 5.938 | 5.687 | 5.453 | 5.234 | 5.029 | 4.836 | 4.656 | 4.486 | 4.327 |
| 12     | 11.255 | 10.575 | 9.954  | 9.385  | 8.863  | 8.384  | 7.943  | 7.536  | 7.161  | 6.814 | 6.492 | 6.194 | 5.918 | 5.660 | 5.421 | 5.197 | 4.988 | 4.793 | 4.611 | 4.439 |
| 13     | 12.134 | 11.348 | 10.635 | 9.986  | 9.394  | 8.853  | 8.358  | 7.904  | 7.487  | 7.103 | 6.750 | 6.424 | 6.122 | 5.842 | 5.583 | 5.342 | 5.118 | 4.910 | 4.715 | 4.533 |
| 14     | 13.004 | 12.106 | 11.296 | 10.563 | 9.899  | 9.295  | 8.745  | 8.244  | 7.786  | 7.367 | 6.982 | 6.628 | 6.302 | 6.002 | 5.724 | 5.468 | 5.229 | 5.008 | 4.802 | 4.611 |
| 15     | 13.865 | 12.849 | 11.938 | 11.118 | 10.380 | 9.712  | 9.108  | 8.559  | 8.061  | 7.606 | 7.191 | 6.811 | 6.462 | 6.142 | 5.847 | 5.575 | 5.324 | 5.092 | 4.876 | 4.675 |
| 16     | 14.718 | 13.578 | 12.561 | 11.652 | 10.838 | 10.106 | 9.447  | 8.851  | 8.313  | 7.824 | 7.379 | 6.974 | 6.604 | 6.265 | 5.954 | 5.668 | 5.405 | 5.162 | 4.938 | 4.730 |
| 17     | 15.562 | 14.292 | 13.166 | 12.166 | 11.274 | 10.477 | 9.763  | 9.122  | 8.544  | 8.022 | 7.549 | 7.120 | 6.729 | 6.373 | 6.047 | 5.749 | 5.475 | 5.222 | 4.990 | 4.775 |
| 18     | 16.398 | 14.992 | 13.754 | 12.659 | 11.690 | 10.828 | 10.059 | 9.372  | 8.756  | 8.201 | 7.702 | 7.250 | 6.840 | 6.467 | 6.128 | 5.818 | 5.534 | 5.273 | 5.033 | 4.812 |
| 19     | 17.226 | 15.678 | 14.324 | 13.134 | 12.085 | 11.158 | 10.336 | 9.604  | 8.950  | 8.365 | 7.839 | 7.366 | 6.938 | 6.550 | 6.198 | 5.877 | 5.584 | 5.316 | 5.070 | 4.843 |
| 20     | 18.046 | 16.351 | 14.877 | 13.590 | 12.462 | 11.470 | 10.594 | 9.818  | 9.129  | 8.514 | 7.963 | 7.469 | 7.025 | 6.623 | 6.259 | 5.929 | 5.628 | 5.353 | 5.101 | 4.870 |
| 25     | 22.023 | 19.523 | 17.413 | 15.622 | 14.094 | 12.783 | 11.654 | 10.675 | 9.823  | 9.077 | 8.422 | 7.843 | 7.330 | 6.873 | 6.464 | 6.097 | 5.766 | 5.467 | 5.195 | 4.948 |
| 30     | 25.808 | 22.396 | 19.600 | 17.292 | 15.372 | 13.765 | 12.409 | 11.258 | 10.274 | 9.427 | 8.694 | 8.055 | 7.496 | 7.003 | 6.566 | 6.177 | 5.829 | 5.517 | 5.235 | 4.979 |
| 35     | 29.409 | 24.999 | 21.487 | 18.665 | 16.374 | 14.498 | 12.948 | 11.655 | 10.567 | 9.644 | 8.855 | 8.176 | 7.586 | 7.070 | 6.617 | 6.215 | 5.858 | 5.539 | 5.251 | 4.992 |
| 40     | 32.835 | 27.355 | 23.115 | 19.793 | 17.159 | 15.046 | 13.332 | 11.925 | 10.757 | 9.779 | 8.951 | 8.244 | 7.634 | 7.105 | 6.642 | 6.233 | 5.871 | 5.548 | 5.258 | 4.997 |
| 50     | 39.196 | 31.424 | 25.730 | 21.482 | 18.256 | 15.762 | 13.801 | 12.233 | 10.962 | 9.915 | 9.042 | 8.304 | 7.675 | 7.133 | 6.661 | 6.246 | 5.880 | 5.554 | 5.262 | 4.999 |